

# Markscheme

May 2018

Mathematical studies

Standard level

Paper 1

23 pages

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**Paper 1 Markscheme  
Instructions to Examiners**

**Notes:** If in doubt about these instructions or any other marking issues, contact your team leader for clarification.

The number of marks for each question is 6.

**1 Abbreviations**

The markscheme may make use of the following abbreviations:

- M** Marks awarded for **Method**
- A** Marks awarded for an **Answer** or for **Accuracy**
- C** Marks awarded for **Correct** answers (irrespective of working shown)
- R** Marks awarded for clear **Reasoning**
- ft** Marks that can be awarded as **follow through** from previous results in the question

**2 Method of Marking**

- (a) All marking must be done in RM Assessor using the mathematical studies annotations and in accordance with the current document for guidance in e-marking Mathematical Studies SL. It is essential that you read this document before you start marking.
- (b) If the candidate has full marks on a question use the **C6** annotation, if the candidate has made an attempt but scores zero marks use **C0**. If there is no attempt use the No response button. If a candidate does not score full or zero marks then full annotations **MUST** be shown.
- (c) In this paper, if the **correct answer is seen on the answer line the** maximum mark is awarded. **There is no need to check the working!** Award **C** marks and move on.
- (d) If the answer does not appear on the answer line, but the correct answer is seen in the working box with no subsequent working, award the maximum mark.
- (e) If the **answer is wrong**, marks should be awarded for the working according to the markscheme.
- (f) Working crossed out by the candidate should not be awarded any marks. Where candidates have written two solutions to a question, only the first solution should be marked.
- (g) A correct answer in the working box transcribed inaccurately to the answer line can receive full marks.
- (h) If correct working results in a correct answer **in the working box** but then further working is developed, indicating a lack of mathematical understanding full marks should **not** be awarded. In most such cases it will be a single final answer mark that is lost, however, a statement on the answer line should always be taken as the candidate's final decision on the answer **as long as it is unambiguous**. An exception to this may be in numerical answers, where a correct exact value is followed by an incorrect decimal.

Example:

	Correct answer seen	Further working seen	Action
1.	$8\sqrt{2}$	5.65685... (incorrect decimal value)	Award the final <b>(A1)</b> (ignore the further working)
2.	$(x - 6)(x + 1)$	$x = 6$ and $-1$	Do <b>not</b> award the final <b>(A1)</b> (see next example)

**Example:** Factorise  $x^2 - 5x - 6$

Markscheme	Candidates' Scripts	Marking
$(x - 6)(x + 1)$ <b>(A1)(A1)</b>	(i) Answer line: $(x + 6)(x + 1)$	<b>(A0)(A1)</b>
	(ii) Working box: $(x - 6)(x + 1)$ followed by $x = 6$ and $-1$ , or just $6, -1$ in either working box or on answer line.	<b>(A1)</b>
		<b>(A0)</b>

### 3 Follow through (ft) Marks

Errors made at any step of a solution affect all working that follows. To limit the severity of the penalty, **follow through (ft)** marks can be awarded. Markschemes will indicate where it is appropriate to apply follow through in a question with '(ft)'.

- (a) Follow through applies only from one part of a question to a subsequent part of the question. Follow through does not apply within the same part.
- (b) If an answer resulting from follow through is extremely unrealistic (eg, negative distances or incorrect by large order of magnitude) then the final **A** mark should not be awarded.
- (c) If a question is transformed by an error into a **different, much simpler question** then follow through may not apply.
- (d) To award follow through marks for a question part, **there must be working present for that part**. An isolated follow through answer, without working is regarded as incorrect and receives no marks **even if it is approximately correct**.
- (e) The exception to the above would be in a question which is testing the candidate's use of the GDC, where working will not be expected. **The markscheme will clearly indicate where this applies**.
- (f) Inadvertent use of radians will be penalised the first time it occurs. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for the use of radians.

**Example:** Finding angles and lengths using trigonometry

Markscheme	Candidates' Scripts	Marking
(a) $\frac{\sin A}{3} = \frac{\sin 30}{4}$ <b>(M1)(A1)</b>  $A = 22.0^\circ$ (22.0243...) <b>(A1)</b>	(a) $\frac{\sin A}{4} = \frac{\sin 30}{3}$	<b>(M1)(A0)</b>  (use of sine rule but with wrong values)
	$A = 41.8^\circ$ <i>(Note: the 2<sup>nd</sup> (A1) here was not marked (ft) and cannot be awarded because there was an earlier error in the same question part.)</i>	<b>(A0)</b>
(b) $x = 7 \tan (22.0243\dots^\circ)$ <b>(M1)</b> $= 2.83$ (2.83163...) <b>(A1)(ft)</b>	(b) case (i) $x = 7 \tan 41.8^\circ$ $= 6.26$ <b>but</b> case (ii) $6.26$	<b>(M1)</b> <b>(A1)(ft)</b> <b>(C0)</b> since no working shown

#### 4 Using the Markscheme

(a) **A** marks are **dependent** on the preceding **M** mark being awarded, it is **not** possible to award **(M0)(A1)**. Once an **(M0)** has been awarded, all subsequent **A** marks are lost in that part of the question, even if calculations are performed correctly, until the next **M** mark.  
The only exception will be for an answer where the accuracy is specified in the question – see section 5.

(b) **A** marks are **dependent** on the **R** mark being awarded, it is **not** possible to award **(A1)(R0)**. Hence the **(A1)** is not awarded for a correct answer if no reason or the wrong reason is given.

(c) **Alternative methods** may not always be included. Thus, if an answer is wrong then the working must be carefully analysed in order that marks are awarded for a different method consistent with the markscheme.  
Where alternative methods for complete questions are included in the markscheme, they are indicated by '**OR**' etc.

(d) Unless the question specifies otherwise, accept **equivalent forms**. For example:  $\frac{\sin \theta}{\cos \theta}$  for  $\tan \theta$ .

On the markscheme, these equivalent numerical or algebraic forms will sometimes be written in brackets after the required answer.

Where numerical answers are required as the final answer to a part of a question in the markscheme, the scheme will show, in order:

the 3 significant figure answer worked through from full calculator display;

the exact value  $\left( \text{for example } \frac{2}{3} \text{ if applicable} \right)$ ;

the full calculator display in the form 2.83163... as in the example above.

Where answers are given to 3 significant figures and are then used in subsequent parts of the question leading to a **different** 3 significant figure answer, these solutions will also be given.

(e) As this is an international examination, all valid **alternative forms of notation** should be accepted. Some examples of these are:

Decimal points: 1.7; 1'7; 1·7; 1,7 .

Decimal numbers less than 1 may be written with or without a leading zero: 0.49 or .49 .

Different descriptions of an interval:  $3 < x < 5$ ; (3, 5); ] 3, 5 [ .

Different forms of notation for set properties (e.g. complement):  $A'$ ;  $\bar{A}$ ;  $A^c$ ;  $U - A$ ;  $(A; U \setminus A$ .

Different forms of logic notation:  $\neg p$ ;  $p'$ ;  $\tilde{p}$ ;  $\bar{p}$ ;  $\sim p$ .

$p \Rightarrow q$ ;  $p \rightarrow q$ ;  $q \Leftarrow p$ .

Significance level may be written as  $\alpha$  .

(f) Discretionary marks: There will be very rare occasions where the markscheme does not cover the work seen. In such cases the annotation DM should be used to indicate where an examiner has used discretion. Discretion should be used sparingly and if there is doubt an exception should be raised through RM Assessor to the team leader.

As with previous sessions there will be no whole paper penalty marks for accuracy AP, financial accuracy FP and units UP. Instead these skills will be assessed in particular questions and the marks applied according to the rules given in sections 5, 6 and 7 below.

### 5 Accuracy of Answers

**Incorrect accuracy should be penalized once only in each question according to the rules below.**

Unless otherwise stated in the question, all numerical answers should be given exactly or correct to 3 significant figures.

1. If the **candidate's answer** is seen to 4 sf or greater **and** would round to the required 3 sf answer, then award **(A1)** and ignore subsequent rounding.

**Note:** The unrounded answer may appear in either the working box or on the final answer line.

2. If the candidate's unrounded answer is **not** seen then award **(A1)** if the answer given is **correctly** rounded to 2 or more significant figures, otherwise **(A0)**.

**Note:** If the candidate's unrounded answer is **not** seen and the answer is given correct to 1 sf (correct or not), the answer will be considered wrong and will not count as incorrect accuracy. If this answer is used in subsequent parts, then working must be shown for further marks to be awarded.

3. If a correct 2 sf answer is used in subsequent parts, then working **must** be shown for further marks to be awarded. (This treatment is the same as for following through from an incorrect answer.)

These 3 points (see numbers in superscript) have been summarized in the table below and illustrated in the examples which follow.

	If candidates final answer is given ...					
	Exact or to 4 or more sf (and would <b>round to the correct 3 sf</b> )	<b>Correct to 3 sf</b>	<b>Incorrect to 3 sf</b>	Correct to 2 sf <sup>3</sup>	Incorrect to 2 sf	Correct or incorrect to 1 sf
Unrounded answer seen <sup>1</sup>	Award the final <b>(A1)</b> irrespective of correct or incorrect rounding					
Unrounded answer not seen <sup>2</sup>	<b>(A1)</b>	<b>(A1)</b>	<b>(A0)</b>	<b>(A1)</b>	<b>(A0)</b>	<b>(A0)</b>
Treatment of subsequent parts	As per MS		Treat as follow through, only if working is seen. <sup>3</sup>			

Examples:

Markscheme	Candidates' Scripts	Marking
9.43 (9.43398...) <b>(A1)</b>	(i) 9.43398... is seen in the working box followed by 9; 9.4; 9.43; 9.434 etc. (correctly rounded)	<b>(A1)</b>
	(ii) 9.43398... is seen in the working box followed by 9.433; 9.44 etc. (incorrectly rounded)	<b>(A1)</b>
	(iii) 9.4	<b>(A1)</b>
	(iv) 9	<b>(A0)</b> <i>(correct to 1 sf)</i>
	(v) 9.3	<b>(A0)</b> <i>(incorrectly rounded to 2 sf)</i>
	(vi) 9.44	<b>(A0)</b> <i>(incorrectly rounded to 3 sf)</i>

Markscheme	Candidates' Scripts	Marking
7.44 (7.43798...) <b>(A1)</b>	(i) 7.43798... is seen in the working box followed by 7; 7.4; 7.44; 7.438 etc. (correctly rounded)	<b>(A1)</b>
	(ii) 7.43798... is seen in the working box followed by 7.437; 7.43 etc. (incorrectly rounded)	<b>(A1)</b>
	(iii) 7.4	<b>(A1)</b>
	(iv) 7	<b>(A0)</b> <i>(correct to 1 sf)</i>
	(v) 7.5	<b>(A0)</b> <i>(incorrectly rounded to 2 sf)</i>
	(vi) 7.43	<b>(A0)</b> <i>(incorrectly rounded to 3 sf)</i>

**Example:** ABC is a right angled triangle with angle  $\angle C = 90^\circ$ , AC = 32 cm and AB = 30 cm. Find (a) the length of BC, (b) The area of triangle ABC.

Markscheme	Candidates' Scripts	Marking
(a) $BC = \sqrt{32^2 - 30^2}$ <b>(M1)</b> Award <b>(M1)</b> for correct substitution in Pythagoras' formula  $= 11.1 (\sqrt{124}, 11.1355\dots)(\text{cm})$ <b>(A1)</b>	(a) $BC = \sqrt{32^2 - 30^2}$  11 (cm)  <i>(2 sf answer only seen, but correct)</i>	<b>(M1)</b>  <b>(A1)</b>
(b) $\text{Area} = \frac{1}{2} \times 30 \times 11.1355\dots$ <b>(M1)</b> Award <b>(M1)</b> for correct substitution in area of triangle formula  $= 167(167.032\dots)(\text{cm}^2)$ <b>(A1)(ft)</b>	(b) case (i) $\text{Area} = \frac{1}{2} \times 30 \times 11$  $= 165 (\text{cm}^2)$  case (ii) $= 165 (\text{cm}^2)$  <i>(No working shown, the answer 11 is treated as a ft, so no marks awarded here)</i>	<b>(M1)</b>  <i>(working shown)</i>  <b>(A1)(ft)</b>  <b>(M0)(A0)(ft)</b>

Rounding of an exact answer to 3 significant figures **should be accepted if performed correctly**.

Exact answers such as  $\frac{1}{4}$  can be written as decimals to fewer than 3 significant figures if the result is still exact. Reduction of a fraction to its lowest terms is **not** essential, however where an answer simplifies to an integer this is expected. Fractions that include a decimal in the numerator and/or the denominator are acceptable for showing correct substitution, but not as a final answer.

Ratios of  $\pi$  and answers taking the form of square roots of integers or any rational power of an integer (e.g.  $\sqrt{13}, 2^{\frac{2}{3}}, \sqrt[4]{5}$ , ...) may be accepted as exact answers. All other powers (eg, of non-integers) and values of transcendental functions such as sine and cosine must be evaluated.

**If the level of accuracy is specified in the question, a mark will be allocated for giving the answer to the required accuracy.** In **all** such cases the final mark is not awarded if the rounding does not follow the instructions given in the question. A mark for specified accuracy can be regarded as a **(ft)** mark regardless of an immediately preceding **(M0)**.



Certain answers obtained from the GDC are worth 2 marks and working will not be seen. In these cases only one mark should be lost for accuracy.

eg, Chi-squared, correlation coefficient, mean

Markscheme	Candidates' Scripts	Marking
Chi-squared	(a) 7.7	<b>(A2)</b>
7.68 (7.67543...) <b>(A2)</b>	(b) 7.67	<b>(A1)</b>
	(c) 7.6	<b>(A1)</b>
	(d) 8	<b>(A0)</b>
	(e) 7	<b>(A0)</b>
	(e) 7.66	<b>(A0)</b>

Regression line

Markscheme	Candidates' Scripts	Marking
$y = 0.888x + 13.5$ <b>(A2)</b> ( $y = 0.887686...x + 13.4895...$ ) If an answer is not in the form of an equation award at most <b>(A1)(A0)</b> .	(a) $y = 0.89x + 13$	<b>(A2)</b> <i>(both accepted)</i>
	(b) $y = 0.88x + 13$	<b>(A1)</b> <i>(one rounding error)</i>
	(c) $y = 0.88x + 14$	<b>(A1)</b> <i>(rounding error repeated)</i>
	(d) (i) $y = 0.9x + 13$	<b>(A1)</b> <i>(1 sf not accepted)</i>
	(ii) $y = 0.8x + 13$	
	(e) $0.88x + 14$	<b>(A0)</b> <i>(two rounding errors and not an equation)</i>

Maximum/minimum/points of intersection

Markscheme	Candidates' Scripts	Marking
(2.06, 4.49) <b>(A1)(A1)</b> (2.06020..., 4.49253...)	(a) (2.1, 4.5)	<b>(A1)(A1)</b> <i>(both accepted)</i>
	(b) (2.0, 4.4)	<b>(A1)</b> <i>(same rounding error twice)</i>
	(c) (2.06, 4.4)	<b>(A1)</b> <i>(one rounding error)</i>
	(d) (2, 4.4)	<b>(A0)</b> <i>(1sf not accepted, one rounding error)</i>

### 6 Level of accuracy in finance questions

The accuracy level required for answers will be specified in all questions involving money. This will usually be either whole units or two decimal places. The first answer not given to the specified level of accuracy will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one mark per paper can be lost for incorrect accuracy in a financial question.

**Example:** A financial question demands accuracy correct to 2 dp.

Markscheme	Candidates' Scripts	Marking
\$231.62 (231.6189) <b>(A1)</b>	(i) 231.6	<b>(A0)</b>
	(ii) 232	<b>(A0)</b> <i>(Correct rounding to incorrect level)</i>
	(iii) 231.61	<b>(A0)</b>
	(iv) 232.00	<b>(A0)</b> <i>(Parts (iii) and (iv) are both incorrect rounding to correct level)</i>

### 7 Units in answers

There will be specific questions for which the units are required and this will be indicated clearly in the markscheme. The first correct answer with no units or incorrect units will not be awarded the final **A** mark. The markscheme will give clear instructions to ensure that only one or two marks per paper can be lost for lack of units or incorrect units.

The units are considered only when the numerical answer is awarded **(A1)** under the accuracy rules given in Section 5.

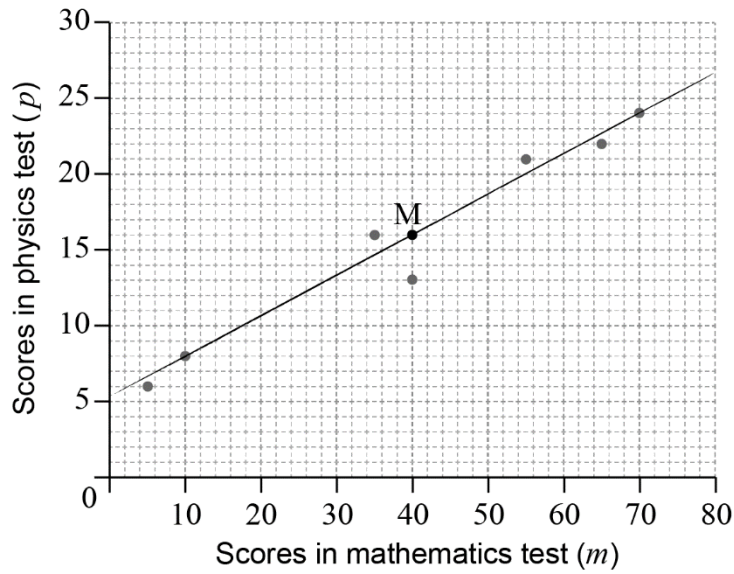
Markscheme	Candidates' Scripts	Marking
(a) 37000 m <sup>2</sup> <b>(A1)</b>	(a) 36000 m <sup>2</sup>	<b>(A0)</b> <i>(Incorrect answer so units not considered)</i>
(b) 3200 m <sup>3</sup> <b>(A1)</b>	(b) 3200 m <sup>2</sup>	<b>(A0)</b> <i>(Incorrect units)</i>

If no method is shown and the answer is correct but with incorrect or missing units award the C marks with a one mark penalty.

### 8 Graphic Display Calculators

Candidates will often obtain solutions directly from their calculators. They must use mathematical notation, not calculator notation. No method marks can be awarded for incorrect answers supported only by calculator notation. The comment "I used my GDC" cannot receive a method mark.

1. (a)



(A1)(A1) (C2)

**Note:** Award (A1) for mean point plotted and (A1) for labelled M.

[2 marks]

(b) straight line through their mean point crossing the *p*-axis at  $5 \pm 2$

(A1)(ft)(A1)(ft) (C2)

**Note:** Award (A1)(ft) for a **straight** line through their **mean** point.  
Award (A1)(ft) for a correct *p*-intercept if line is extended.

[2 marks]

(c) point on line where  $m = 20$  identified and an attempt to identify *y*-coordinate (M1)  
10.5 (A1)(ft) (C2)

**Note:** Follow through from their line in part (b).

[2 marks]

**Total [6 marks]**

2. (a) if the baby is happy and wants to play then the baby does not cry (A1)(A1)(A1) (C3)

**Note:** Award (A1) for “If... then...”; (A1) for “the baby is happy **and** wants to play”, (A1) for “the baby does not cry”. Crying must be negated.

[3 marks]

(b)

$p$	$q$	$r$	$\neg p$	$q \wedge r$	$(q \wedge r) \Rightarrow \neg p$
T	T	T	F	<b>T</b>	<b>F</b>
T	T	F	F	<b>F</b>	<b>T</b>
T	F	T	F	<b>F</b>	<b>T</b>
T	F	F	F	<b>F</b>	<b>T</b>
F	T	T	T	<b>T</b>	<b>T</b>
F	T	F	T	<b>F</b>	<b>T</b>
F	F	T	T	<b>F</b>	<b>T</b>
F	F	F	T	<b>F</b>	<b>T</b>

(A1)(A1) (C2)

**Note:** Award (A1) for each correct column.

[2 marks]

- (c) Neither (A1)(ft) (C1)

**Note:** Follow through from the last column in their part (b).

[1 mark]

**Total [6 marks]**

3. (a)  $4.8 \times 10^8 \times 2.5$  (M1)

**Note:** Award (M1) for multiplying by 2.5.

$1.2 \times 10^9$  (cm) (A1)(ft)(A1)(ft) (C3)

**Note:** Award (A0)(A0) for answers of the type  $12 \times 10^8$ .

[3 marks]

(b) (i) 640 000 000 (cm) ( $6.4 \times 10^8$  (cm)) (A1)

(ii)  $\frac{1.2 \times 10^9}{6.4 \times 10^8}$  (M1)

**Note:** Award (M1) for division by 640 000 000.

= 1.88 (1.875) (A1)(ft) (C3)

**Note:** Follow through from part (a) and part (b)(i).

[3 marks]

Total [6 marks]

4. (a)

Set	Example of a number in the set
N	<b>Any natural number</b>
Z	<b>Any integer</b>
Q	<b>Any rational number</b>
R	<b>Any real number</b>

(A1)(A1)(A1)(A1)(C4)  
[4 marks]

(b) Incorrect (A1)

Natural numbers are positive integers. Integers can also be negative. (or equivalent) (R1) (C2)

**Note:** Accept a correct justification. Do not award (R0)(A1).  
Accept: a statement with an example of an integer which is not natural.

[2 marks]

Total [6 marks]

5. (a) (i)  $1000\left(1 + \frac{3.5}{4 \times 100}\right)^{4 \times 5}$  **(M1)(A1)**

**Note:** Award **(M1)** for substitution in compound interest formula, **(A1)** for correct substitution.

**OR**

$N = 5$   
 $I = 3.5$   
 $PV = 1000$   
 $P/Y = 1$   
 $C/Y = 4$

**Note:** Award **(A1)** for  $C/Y = 4$  seen, **(M1)** for other correct entries.

**OR**

$N = 5 \times 4$   
 $I = 3.5$   
 $PV = 1000$   
 $P/Y = 4$   
 $C/Y = 4$

**Note:** Award **(A1)** for  $C/Y = 4$  seen, **(M1)** for other correct entries.

= 1190.34 (USD) **(A1)**

**Note:** Award **(M1)** for substitution in compound interest formula, **(A1)** for correct substitution.

(ii) 190.34 (USD) **(A1)(ft)** **(C4)**

**Note:** Award **(A1)(ft)** for subtraction of 1000 from their part (a)(i).  
 Follow through from (a)(i).

**[4 marks]**

(b)  $\frac{170}{190.34}$  **(M1)**

**Note:** Award **(M1)** for division of 170 by their part (a)(ii).

= 0.89 **(A1)(ft)** **(C2)**

**Note:** Follow through from their part (a)(ii).

**[2 marks]**

**Total [6 marks]**

6. (a)  $0 = 10a + 5$  **(M1)**

**Note:** Award **(M1)** for correctly substituting any point from  $L_1$  into the equation.

**OR**

$$\frac{0-5}{10-0} \quad \text{**(M1)**}$$

**Note:** Award **(M1)** for correctly substituting any two points on  $L_1$  into the gradient formula.

$$-\frac{5}{10} \left( -\frac{1}{2}, -0.5 \right) \quad \text{**(A1)** **(C2)**}$$

**[2 marks]**

(b)  $(-1.33, 5.67) \left( \left( -\frac{4}{3}, \frac{17}{3} \right), \left( -1\frac{1}{3}, 5\frac{2}{3} \right), (-1.33333\dots, 5.66666\dots) \right)$

**(A1)(ft)(A1)(ft) **(C2)****

**Note:** Award **(A1)** for  $x$ -coordinate and **(A1)** for  $y$ -coordinate. Follow through from their part (a). Award **(A1)(A0)** if brackets are missing. Accept  $x = -1.33, y = 5.67$ .

**[2 marks]**

(c)  $3 = -2(2) + c$  **(M1)**

**Note:** Award **(M1)** for correctly substituting  $-2$  and the given point into the equation of a line.

$$y = -2x + 7 \quad \text{**(A1)** **(C2)**}$$

**Note:** Award **(A0)** if the equation is not written in the form  $y = mx + c$ .

**[2 marks]**

**Total [6 marks]**

7. (a) 20 (A1) (C1)  
[1 mark]

(b)  $\frac{5}{43}$  (0.11627..., 11.6279...%) (A1)(A1) (C2)

**Note:** Award (A1) for correct numerator, (A1) for correct denominator.

[2 marks]

(c)  $\frac{7}{37} \times \frac{12}{36} + \frac{12}{37} \times \frac{7}{36}$  (A1)(M1)

**Note:** Award (A1) for first or second correct product seen, (M1) for adding their two products or for multiplying their product by two.

$= \frac{14}{111}$  (0.12612..., 12.6126%) (A1) (C3)

[3 marks]

**Total [6 marks]**

8. (a)  $(AC^2 =) 62^2 + 79^2 - 2 \times 62 \times 79 \times \cos(52^\circ)$  (M1)(A1)

**Note:** Award (M1) for substituting in the cosine rule formula, (A1) for correct substitution.

63.7 (63.6708...) (km) (A1) (C3)

[3 marks]

(b)  $\frac{1}{2} \times 62 \times 79 \times \sin(52^\circ)$  (M1)(A1)

**Note:** Award (M1) for substituting in the area of triangle formula, (A1) for correct substitution.

1930 km<sup>2</sup> (1929.83... km<sup>2</sup>) (A1) (C3)

[3 marks]

**Total [6 marks]**



9. (a) (i)  $A'$  (A1)

**Note:** Accept alternative set notation for complement such as  $U - A$ .

(ii)  $C \cap D'$  OR  $D' \cap C$  (A1)

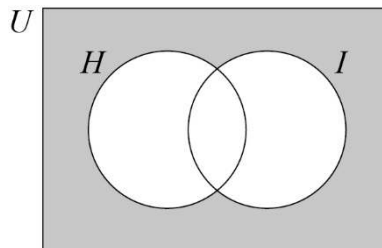
**Note:** Accept alternative set notation for complement.

(iii)  $(E \cap F) \cup G$  OR  $G \cup (E \cap F)$  (A2) (C4)

**Note:** Accept equivalent answers, for example  $(E \cup G) \cap (F \cup G)$ .

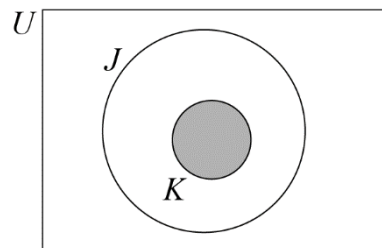
[4 marks]

(b) (i)



(A1)

(ii)



(A1) (C2)  
[2 marks]

Total [6 marks]

10. (a)  $6400 = A \times 2^4$  (M1)

**Note:** Award (M1) for correct substitution of 4 and 6400 in equation.

$(A =) 400$  (A1) (C2)  
[2 marks]

(b) the initial population **OR** the population at the start of experiment (A1) (C1)  
[1 mark]

(c)  $40A = A \times 2^t$  **OR**  $40 \times 400 = 400 \times 2^t$  (M1)

**Note:** Award (M1) for correct substitution into equation.  
Follow through with their  $A$  from part (a).

$40 = 2^t$  (M1)

**Note:** Award (M1) for simplifying.

5.32 (5.32192...) (hours) **OR** 5 hours 19.3 (19.3156...) minutes (A1) (C3)  
[3 marks]

**Total [6 marks]**

11. (a)  $x = 0$  (A1)(A1) (C2)

**Note:** Award (A1) for  $x =$  "a constant" (A1) for  $= 0$ . Award (A0)(A0) for an answer of "0".

[2 marks]

(b)  $f(x) = -2$  ( $y = -2$ ) (A1)(A1) (C2)

**Note:** Award (A1) for  $y =$  "a constant" (A1) for  $= -2$ . Award (A0)(A0) for an answer of "-2".

[2 marks]

(c)  $\frac{3}{x} - 2 = 0$  (M1)

**Note:** Award (M1) for equating  $f(x)$  to 0.

$(x =) \frac{3}{2}$  (1.5) (A1) (C2)  
[2 marks]

**Total [6 marks]**

12. (a) 12.5

(A1) (C1)  
[1 mark]

(b) (i)  $33+k$  OR  $10+8+5+10+k$

(A1)

**Note:** Award (A1) for “number of customers =  $33+k$ ”.

(ii) 
$$\frac{2.5 \times 10 + 7.5 \times 8 + \dots + 22.5 \times k}{33+k} = 12$$

(M1)(A1)(ft)

**Note:** Award (M1) for substitution into the mean formula and equating to 12, (A1)(ft) for their correct substitutions.

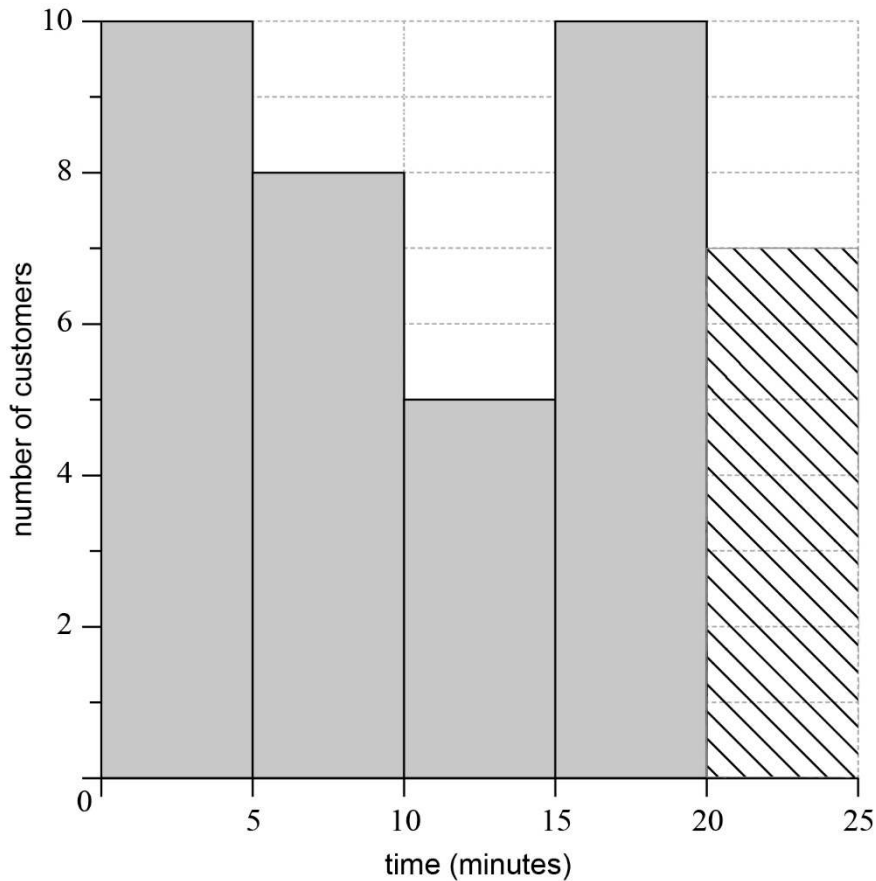
(k =) 7

(A1)(ft) (C4)

**Note:** Follow through from part (b)(i) and their mid-interval values, consistent with part (a). Do not award final (A1) if answer is not an integer.

[4 marks]

(c)



(A1)(ft) (C1)

**Note:** Follow through from their part (b)(ii) but only if the value is between 1 and 10, inclusive.

[1 mark]

Total [6 marks]

13. (a)  $(70 - 75)^2 + 100$  (M1)

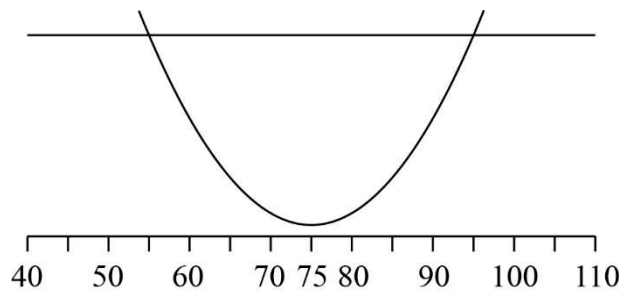
**Note:** Award (M1) for substituting in  $x = 70$ .

125 (A1) (C2)  
[2 marks]

(b)  $(s - 75)^2 + 100 = 500$  (M1)

**Note:** Award (M1) for equating  $C(x)$  to 500. Accept an inequality instead of  $=$ .

OR



(M1)

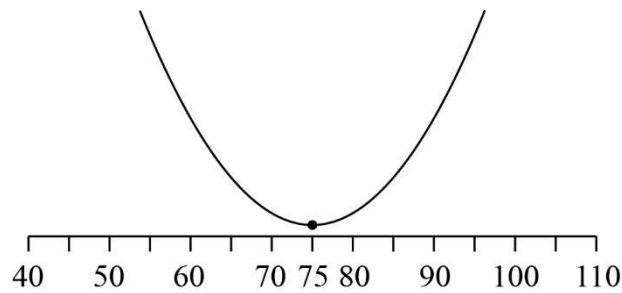
**Note:** Award (M1) for sketching correct graph(s).

$(s =) 95$  (A1) (C2)  
[2 marks]

continued...

Question 13 continued

(c)



(M1)

**Note:** Award (M1) for an attempt at finding the minimum point using graph.

OR

$$\frac{95 + 55}{2}$$

(M1)

**Note:** Award (M1) for attempting to find the mid-point between their part (b) and 55.

OR

$$(C'(x) =) 2x - 150 = 0$$

(M1)

**Note:** Award (M1) for an attempt at differentiation that is correctly equated to zero.

75

(A1) (C2)  
[2 marks]

Total [6 marks]

14. (a)  $x^3$  (A1) (C1)  
[1 mark]

**Note:** Award (A0) for  $\frac{4x^3}{4}$  and not simplified to  $x^3$ .

(b)  $\left(-\frac{1}{2}\right)^3$  (M1)

**Note:** Award (M1) for correct substitution of  $-\frac{1}{2}$  into their derivative.

$-\frac{1}{8}$  (-0.125) (A1)(ft) (C2)

**Note:** Follow through from their part (a).

[2 marks]

(c)  $x^3 = 8$  (A1)(M1)

**Note:** Award (A1) for 8 seen maybe seen as part of an equation  $y = 8x + c$ ,  
(M1) for equating their derivative to 8.

(x =) 2 (A1) (C3)

**Note:** Do not accept (2, 4).

[3 marks]

Total [6 marks]

15. (a) (slant height<sup>2</sup> =)  $10^2 + r^2$  **(M1)**

**Note:** For correct substitution of 10 and  $r$  into Pythagoras' Theorem.

$$\sqrt{10^2 + r^2}$$

**(A1) (C2)**  
**[2 marks]**

(b)  $\pi r^2 + 2\pi r \times 12 + \pi r \sqrt{100 + r^2} = 570$  **(M1)(M1)(M1)**

**Note:** Award **(M1)** for correct substitution in curved surface area of cylinder and area of the base, **(M1)** for their correct substitution in curved surface area of cone, **(M1)** for adding their 3 surface areas and equating to 570. Follow through their part (a).

$= 4.58$  (4.58358...) **(A1)(ft) (C4)**

**Note:** Last line must be seen to award final **(A1)**. Follow through from part (a).

**[4 marks]**

**Total [6 marks]**